
Exponential Convergence of some hp and Tensor FEM

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Abstract

We present recent results in analysis and implementation of hp Finite Element Methods (FEM).

We review

- a) results by M. Dauge and coworkers on analytic regularity theory, and
- b) novel exponential convergence rate bounds of cG and dG hp-FEM.

Recent results and ongoing research on exponential convergence of quantized tensor-formatted first order FEM will also be given.

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